**LIMITS OF FUNCTIONS AS X APPROACHES A CONSTANT**

The following problems require the use of the algebraic computation of limits of functions as x approaches a constant. Most problems are average. A few are somewhat challenging. All of the solutions are given WITHOUT the use of L'Hopital's Rule. If you are going to try these problems before looking at the solutions, you can avoid common mistakes by giving careful consideration to the form during the computations of these limits. Initially, many students INCORRECTLY conclude that is equal to 1 or 0, or that the limit does not exist or is or . In fact, the form is an example of an *indeterminate* form. This simply means that you have *not yet determined* an answer. Usually, this indeterminate form can be circumvented by using algebraic manipulation. Such tools as algebraic simplification, factoring, and conjugates can easily be used to circumvent the form so that the limit can be calculated.

* + *PROBLEM 1 :* Compute .

* + *PROBLEM 2 :* Compute .

* + *PROBLEM 3 :* Compute .

* + *PROBLEM 4 :* Compute .

* + *PROBLEM 5 :* Compute .
  + *PROBLEM 6 :* Compute .

* + *PROBLEM 7 :* Compute .

* + *PROBLEM 8 :* Compute .

* + *PROBLEM 9 :* Compute .

* + *PROBLEM 10 :* Compute . .

* + *PROBLEM 11 :* Compute .

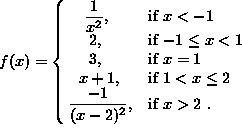
* + *PROBLEM 12 :* Compute .

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* + *PROBLEM 13 :* Compute .

This problem requires an unusual replacement, trigonometry identities, and trigonometry limits.

**The next problem requires an understanding of one-sided limits.**

* + *PROBLEM 14 :* Consider the function 

i.) Sketch the graph of *f* .

ii.) Determine the following limits.

* + - a.)
    - b.)
    - c.)
    - d.)
    - e.)
    - f.)
    - g.)
    - h.)
    - i.)
    - j.)
    - k.)
    - l.)

* + *PROBLEM 15 :* Consider the function

Determine the values of constants *a* and *b* so that .exists and is equal to f(2).